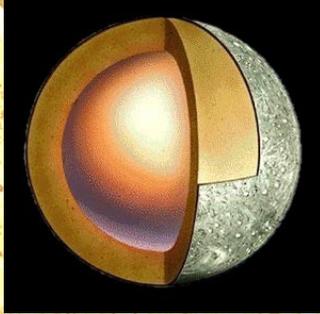


The Magnetosphere of Planet Mercury

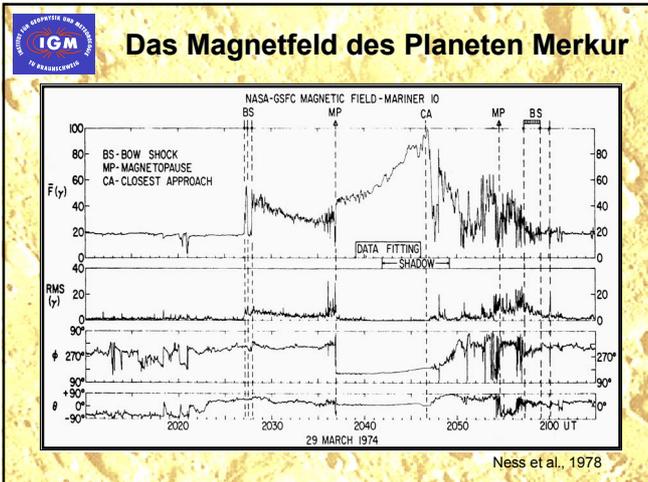


- The planet
- Shape and structure of the magnetosphere
- Current systems
- Dynamics
- Energy sources
- Eigen oscillations

Planet und Magnetfeld



- Planetenradius: 2439 km
- Kernradius: ~1829 km
- Mittl. Dichte: 5.42 g/cm³
- Rotationsrate: 58.64 Tage
- Dipolmoment: 5 · 10¹⁹ Am²
- Ober. Temp.: -173° - 429°
- Atmosphäre: Nein
- Exosphäre: Ja
- Plasmasphäre: Nein
- Magnetosphäre: Ja



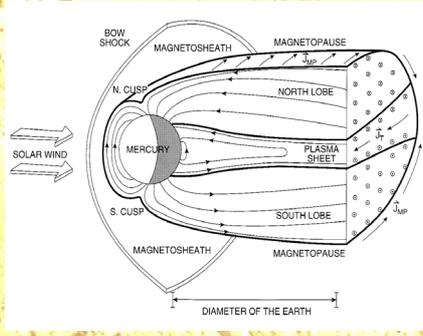
Planetary Magnetic Fields

Planet	Radius [km]	Rotationsperiode [Tage]	Äquatoriales Magnetfeld [nT]
Merkur	2439	58,6	340
Venus	6052	243	0.4
Erde	6371	1	31000
Mars	3397	1	< 0.5
Jupiter	71398	0.4	424000
Braille	0.8	3.6	92500
Saturn	60000	0.41	21500
Uranus	26200	0.72	22800
Neptun	24300	0.70	14400

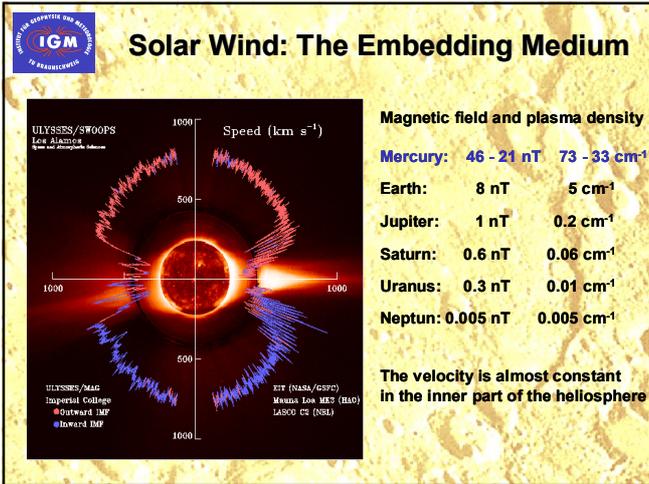
Magnetospheric Plasma Sources

- Mercury:** solar wind and sputtering of surface material, e.g. sodium
- Earth:** solar wind and ionosphere
- Jupiter:** solar wind and volcanic activity of the moon Io
- Saturn:** solar wind, atmosphere of moon Titan, sputtering at surfaces of icy moons and rings
- Uranus:** polar ionosphere, minor solar wind contribution
- Neptun:** ionosphere, moon Triton

The Magnetosphere of Mercury



- No atmosphere
- thus no ionosphere
- but exosphere
- No plasmasphere
- Weak magnetic field
- Multi-ion plasma
- Small magnetosphere



Magnetopause Formation

The magnetopause is a surface where the dynamic pressure of the solar wind and the magnetic pressure of the magnetospheric plasma are in equilibrium:

$$p_{dyn} = 2n_{sw}m_p v_{sw}^2 = \frac{B^2}{2\mu_0}$$

The dynamic pressure of solar wind particles is transferred to the magnetospheric plasma by specular reflection of the particles at the boundary.

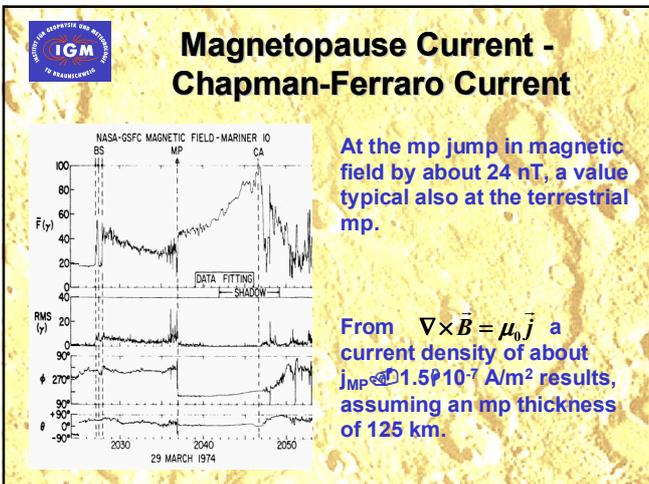
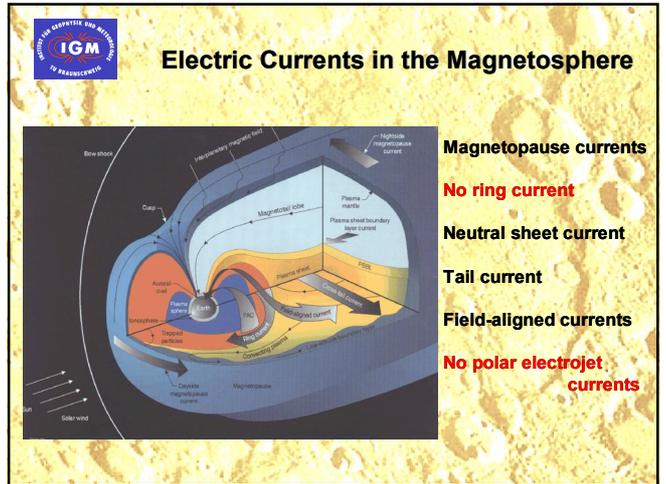
Magnetopause Position

The magnetopause stand-off distance along the Sun-Earth line is given by

$$R_{MP} = \left(\frac{4B_{Surface}^2}{2\mu_0 k n_{sw} m_p v_{sw}^2} \right)^{1/6}$$

where $k = 0.88$ is a correction factor resulting from gasdynamic approximations to the magnetosheath flow:

At Mercury $R_{MP} = 1.5 R_p$



Magnetopause Current – Ground Magnetic Effect

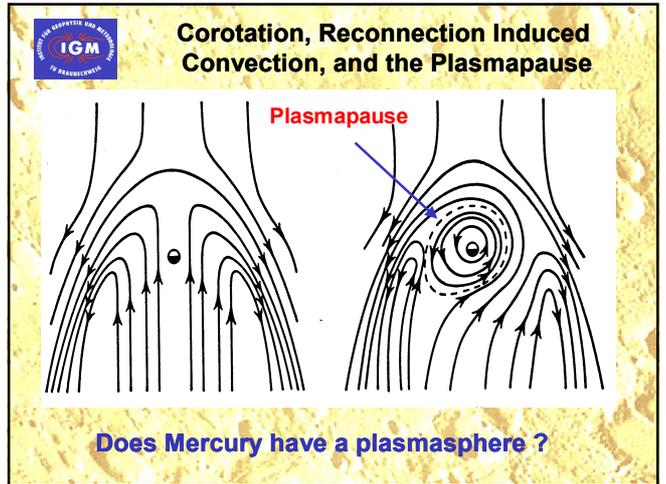
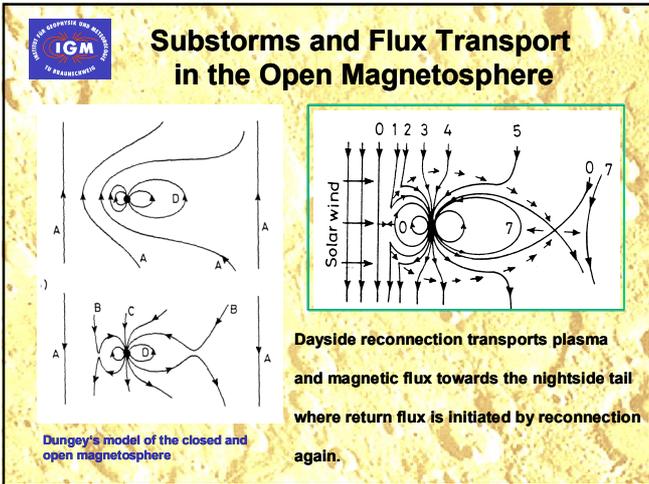
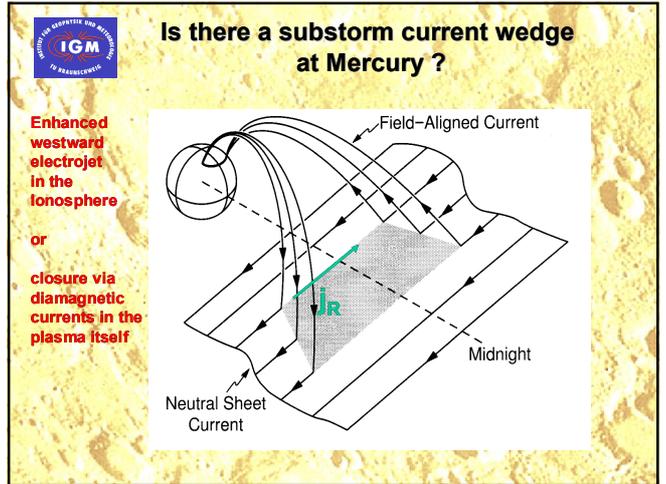
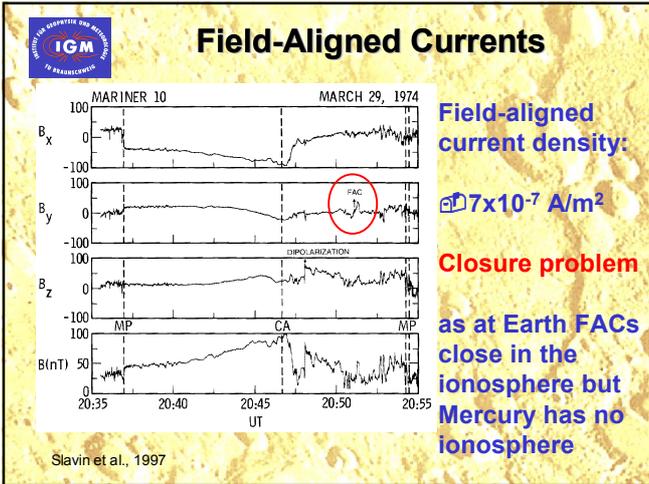
Chapman-Ferraro currents produce ground-magnetic effects, which at

Earth are of the order of 10 nT added to a 30,000 nT background field

and at

Mercury are of the order of 70 nT added to a 340 nT background field

The external field matters at the surface !!!!



Magnetospheric Convection and Corotation

Corotation implies plasma motion and via the frozen-in theorem

$$\vec{E} + \vec{v} \times \vec{B} = 0$$

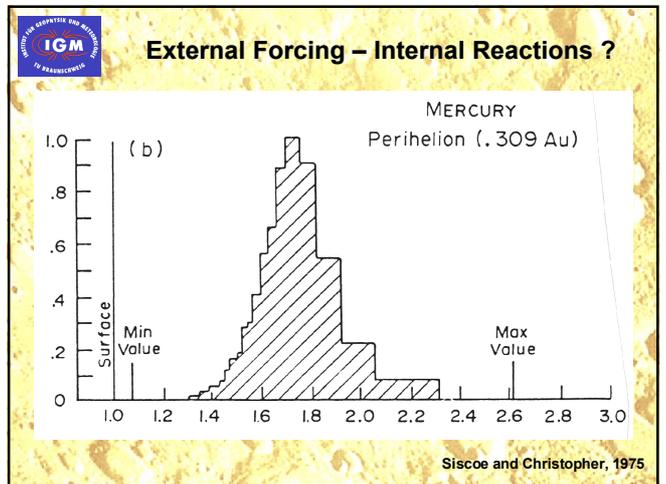
electric fields, that is the corotational electric field is given as

$$\vec{E}_{cor} = - \frac{\Omega_{Earth} B_{surface} R_E^3}{r^2} \vec{e}_r$$

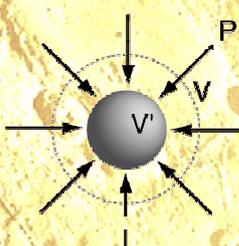
and corotation driven plasma motion is ExB-drift convection

$$\vec{v}_{cor} = \frac{\vec{E}_{cor} \times \vec{B}}{B^2}$$

Mercury has no plasmasphere



IGM **Bulk Modulus and Compressibility**



$$K = V \cdot \frac{\Delta p}{\Delta V}$$

Modulus

$$\kappa = \frac{1}{V} \frac{dV}{dp}$$

Compressibility

IGM **The Magnetospheric Bulk Modulus**

$$R_{MP} = \left(\frac{B_0^2}{\mu_0 p} \right)^{1/6}; \quad p = n_{sw} m_p v_{sw}^2$$
 Magnetopause position

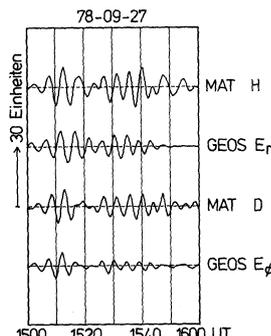
$$K = R_{MP} \cdot \frac{dp}{dR_{MP}} \propto p_{MP}; \quad p_{MP}(r = R_{MP})$$
 Bulk modulus

$$\kappa = 1/K \propto -1/p_{MP}$$
 Compressibility

Mercury has a very stiff, but Jupiter a very fluffy magnetosphere; Mercury rings, Jupiter not !!!!!

IGM **Ringing the Magnetospheric Bell**

78-09-27

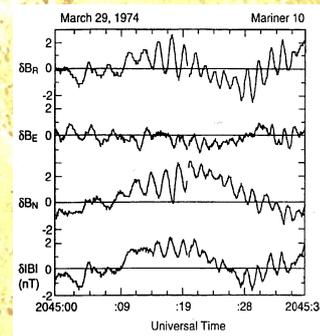


Magnetospheric eigen-oscillations are MHD waves in the terrestrial magnetosphere.

Their periods are much longer than proton gyroperiods !!!

Units: 1 nT; 0.1 mV/m

IGM **ULF Waves at Mercury**



This is the only published evidence for ULF waves in the Hermean magnetosphere.

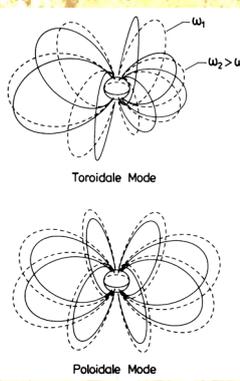
Amplitude: 2 nT

Period: 2 s, e.g. about twice $T_{G,Proton}$

this wave is not an MHD wave !!!!

(from Russell, 1989)

IGM **Global oscillations: The Dungey Problem**



Dipolemagnetosphere

MHD oscillations

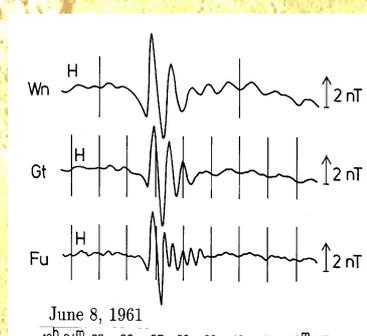
Axisymmetric perturbations

$$\left(\frac{\mu_0 \rho}{B_0^2} \frac{\partial^2}{\partial t^2} - \frac{\partial^2}{\partial r^2} - \frac{\sin \theta}{r^2} \frac{\partial}{\partial \theta} \left(\frac{1}{\sin \theta} \frac{\partial}{\partial \theta} \right) \right) r \sin \theta E_\phi = 0$$

Decoupled toroidal and poloidal oscillations

$$\left(\mu_0 \rho \frac{\partial^2}{\partial t^2} - \frac{1}{r^2 \sin^2 \theta} \left((\vec{B}_0 \cdot \nabla)(r^2 \sin^2 \theta) (\vec{B}_0 \cdot \nabla) \right) \right) \frac{v_\phi}{r \sin \theta} = 0$$

IGM **Global oscillations: Earth**



Decoupled toroidal and poloidal eigen-oscillations for axisymmetric ($m=0$) perturbations

June 8, 1961

13^h 34^m 35 36 37 38 39 40 41 42^m UT

Voelker, 1963

IGM **Global oscillations: Mercury**

To treat this question we need Dungey's equations for a non-MHD model of the Hermean magnetosphere as the anticipated eigenfrequencies are less, but comparable to the gyrofrequency

IGM **Mercury: A Two Component Cold Plasma Approach**

Dielectric Tensor; $0 \ll \omega < \omega_i$

$$\epsilon = \begin{pmatrix} \epsilon_1 & -i\epsilon_2 & 0 \\ i\epsilon_2 & \epsilon_1 & 0 \\ 0 & 0 & \epsilon_3 \end{pmatrix}$$

$$\epsilon_1 \cong \frac{c^2}{v_A^2} + \frac{c^2}{v_A^2} \frac{\omega^2}{\Omega_i^2}; \quad \epsilon_2 \cong -\frac{c^2}{v_A^2} \frac{\omega}{\Omega_i}$$

$$\epsilon_3 \cong -\frac{\omega_{pe}^2}{\omega^2}$$

IGM **Mercury: Global Oscillations Axisymmetric Perturbations m=0**

$\vec{E} = -\nabla_{\perp} \Phi + \nabla_{\perp} \times \Psi \vec{e}_{\parallel}$ **Scalar potentials**

Toroidal operator using curvi-linear coordinates

$$T(\omega) = \partial_3 \frac{g_2}{\sqrt{g}} \partial_3 + \frac{\sqrt{g}}{g_1} \frac{\omega^2}{v_A^2}$$

$\partial_1 T \partial_1 \Phi = i \partial_1 \epsilon_2 \sqrt{\frac{g}{g_1}} \partial_1 \Psi$ **Toroidal oscillation coupled to poloidal though m=0, due to ϵ_2**

=> *Dmitri Klimushkin and Pavel Mager*

IGM **Kinetic Alfvén Waves in the Hermean Magnetosphere**

- Solar wind buffeting causes ringing of the magnetosphere
- The scale of the magnetosphere is about 10 x the ion gyroradius
- Waves generated by buffeting are kinetic Alfvén waves with $E_{\parallel} \cong 0.2 \text{ mV/m}$ (Glassmeier, 2000)
- Buffeting causes particle heating via kinetic Alfvén waves

IGM **Electromagnetic Induction at Mercury**

We have a small magnetosphere

Magnetopause currents are close to the planet

Temporal variations of magnetopause currents may cause strong induction effects

As the planet consists mainly out of a highly conducting core

How large are these induced fields ?

