

# Chromospheric Magnetic Field Measurements

## Challenges & Recent Developments

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**From Measurements towards Understanding**  
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MAX-PLANCK-GESELLSCHAFT



### Summary: measuring chromospheric field is difficult!

- Processes are very fast ( $v_A \approx 100$  km/s, flares, reconnection, ...),
- and occur on small scales (e.g.  $H\alpha$ -fibrillar structure).
- Densities are low.
- Fields are weak  $\rightarrow$  weak signals
- Complex physics  
 $\rightarrow$  loss of simplifying assumptions

## Chromospheric Difficulties

### Loss of simplifying assumptions

- non-LTE
- 3D radiative transfer
- anisotropy of radiation field
- atomic polarization
- additional ambiguities (Hanle)
- many scale-heights
- highly corrugated layers

### Requirements for reliable magnetic field information:

- sophisticated analysis techniques (inversions)  
→ Jaime de la Cruz Rodriguez
- sophisticated treatment of RTE  
→ Han Uitenbroek
- Hanle effect  
→ Javier Trujillo Bueno
- high-quality measurements  
→ this talk

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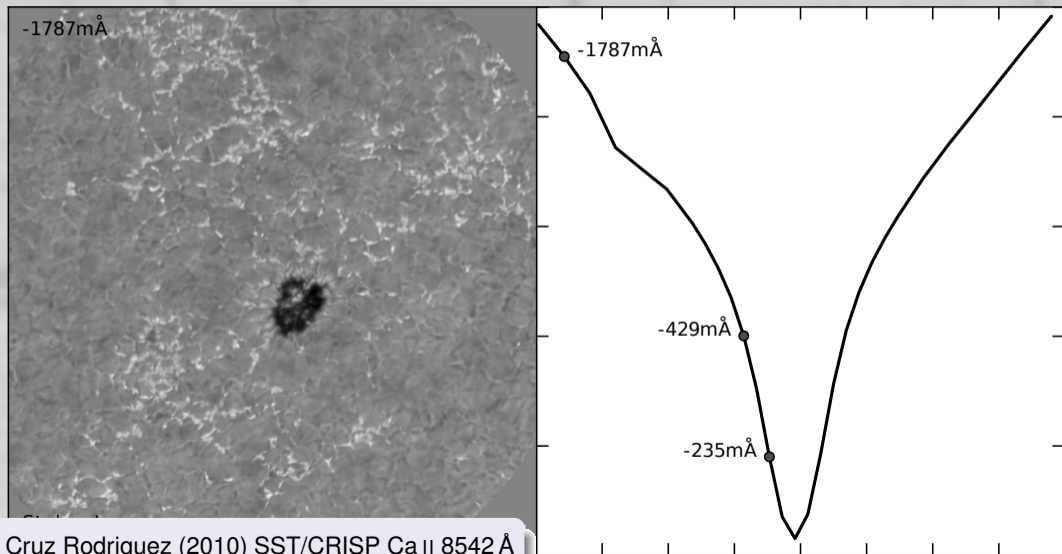
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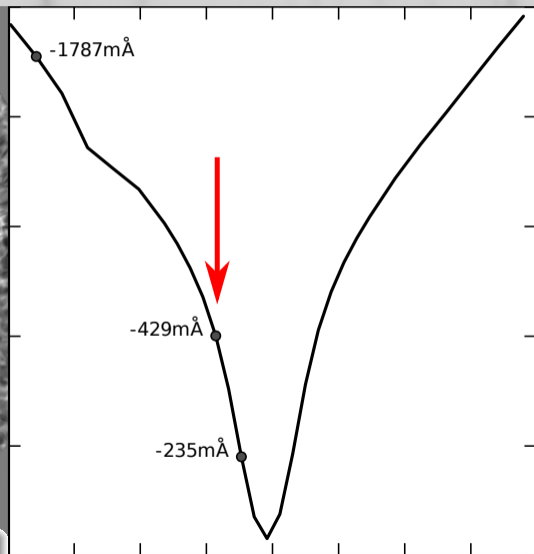
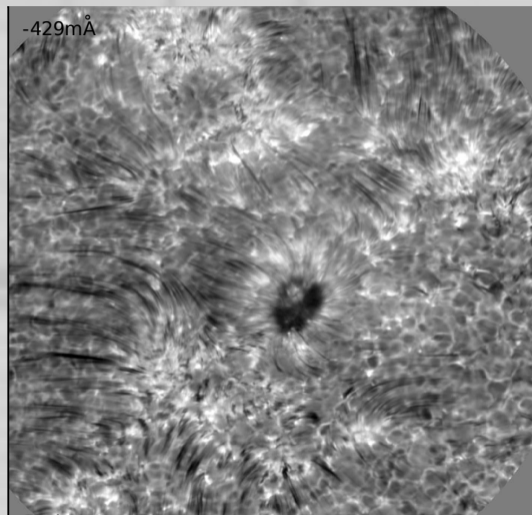
# Low counts, weak signals



de la Cruz Rodriguez (2010) SST/CRISP Ca II 8542 Å

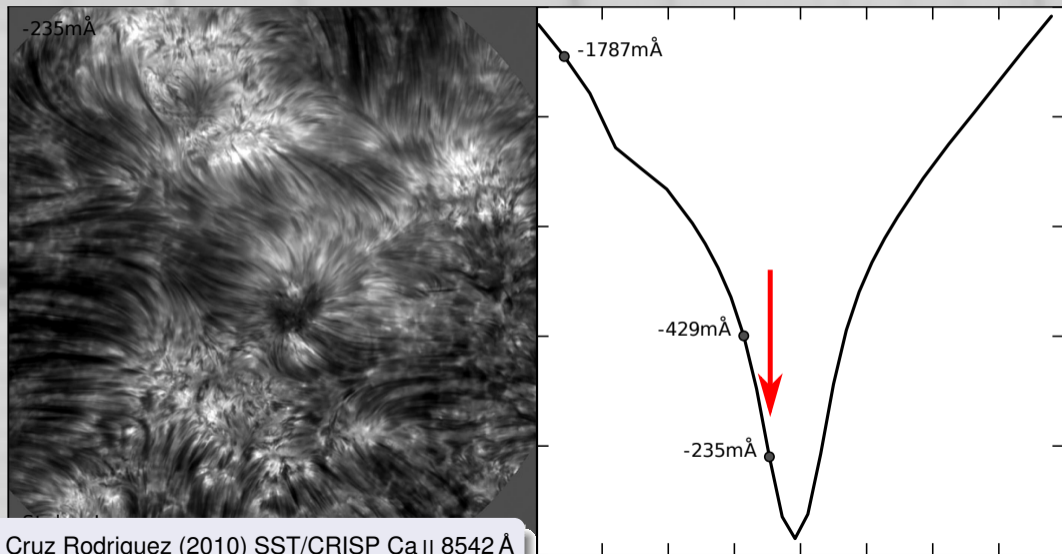


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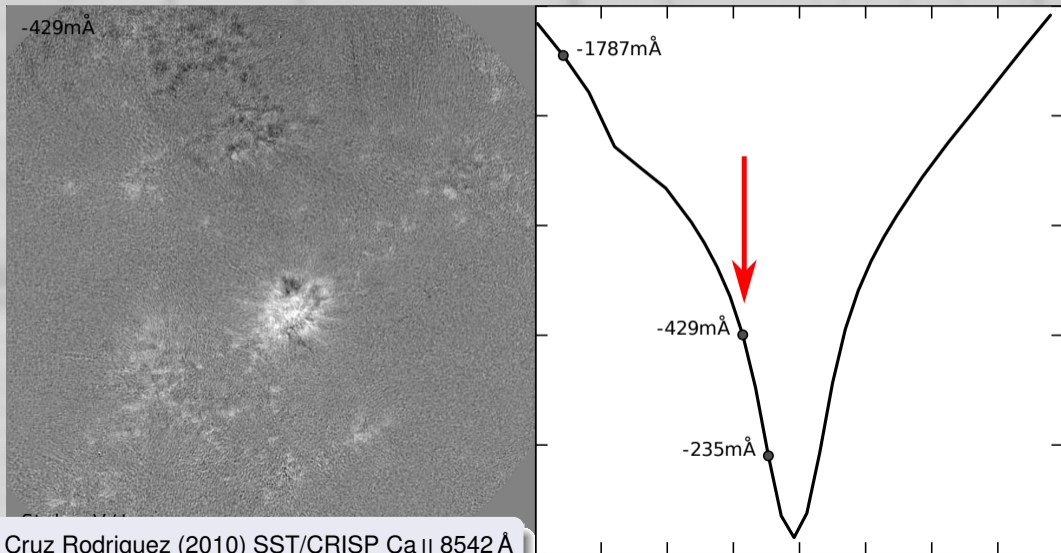
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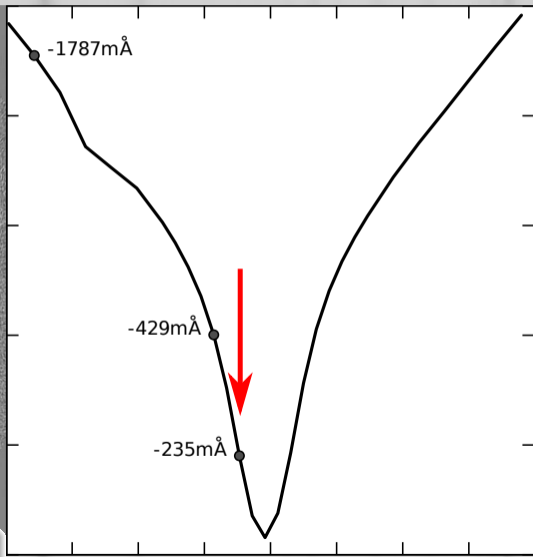
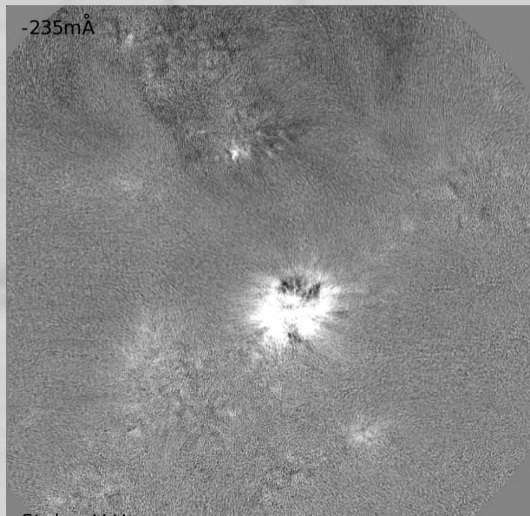
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## Photon budget and solar evolution

## Tradeoff: solar evolution vs. noise:

- **Maximum integration time**  $\Delta t_e$  allowed by solar evolution:

$$\Delta t_e = \frac{2 \Delta x}{v}$$

- **Minimum integration time** to reach a given required rms noise level  $\sigma$ :

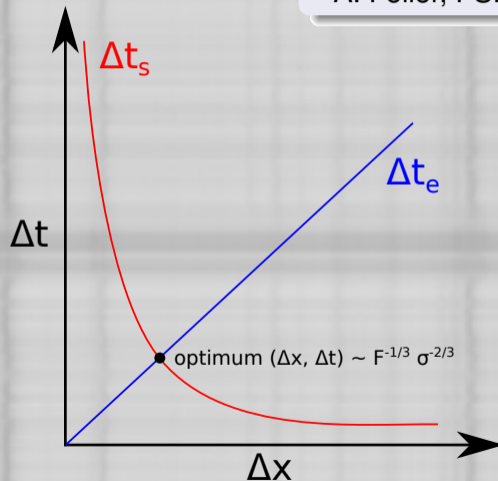
$$\Delta t_s = \frac{1}{F \sigma^2 \Delta x^2}$$

$\Delta x$ : spatial sampling,

$v$ : evolution speed,

$F$ : Flux [phot / (s · arcsec<sup>2</sup>)]

A. Feller, FSP



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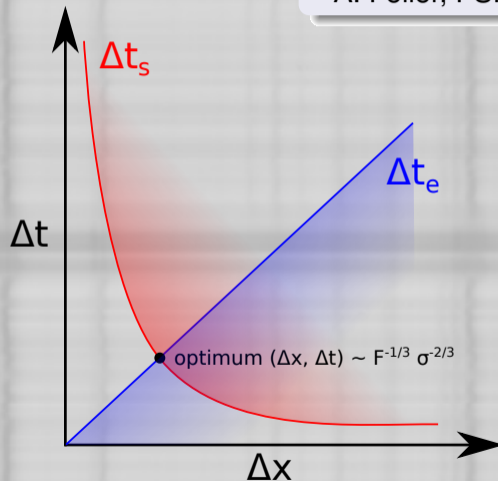
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## Photon budget and solar evolution

## time scales vs. spatial resolution

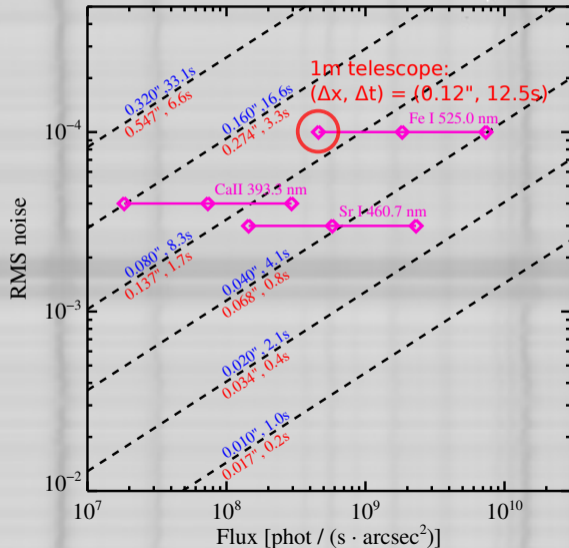
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- chromosphere (red):  $35 \text{ km s}^{-1}$   
( $v_A(B=100 \text{ G}, z=1 \text{ Mm}) = 100 \text{ km s}^{-1}$ )

## Solutions

- 1 stay away from diffraction limit  
→ collect photons
- 2 very fast measurements  
→ “feature averaging”

(Note: solar evolution introduces crosstalk in polarimetry → modulation much faster → FSP)

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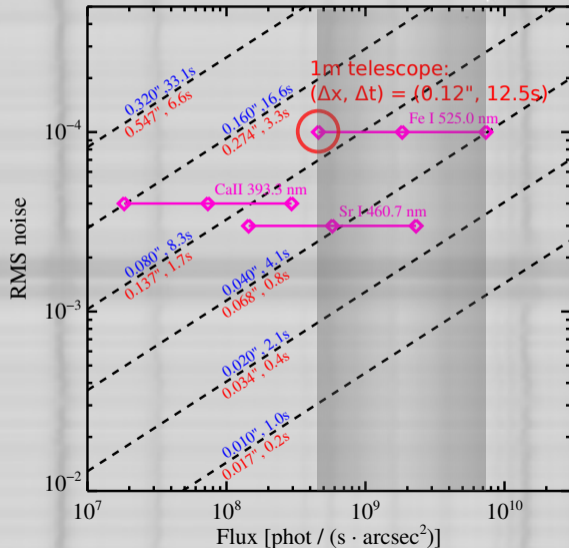
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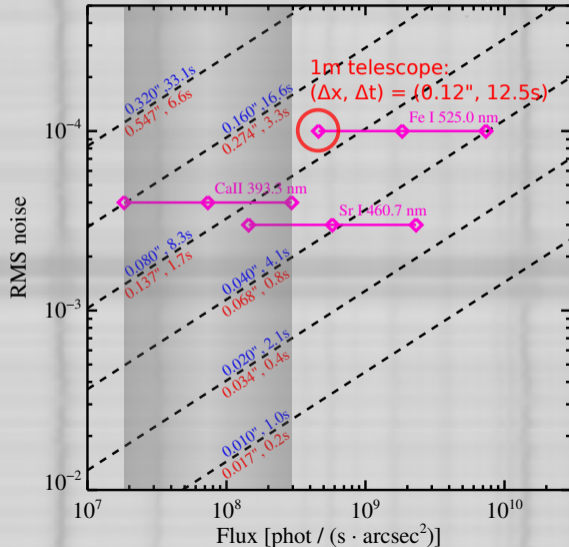
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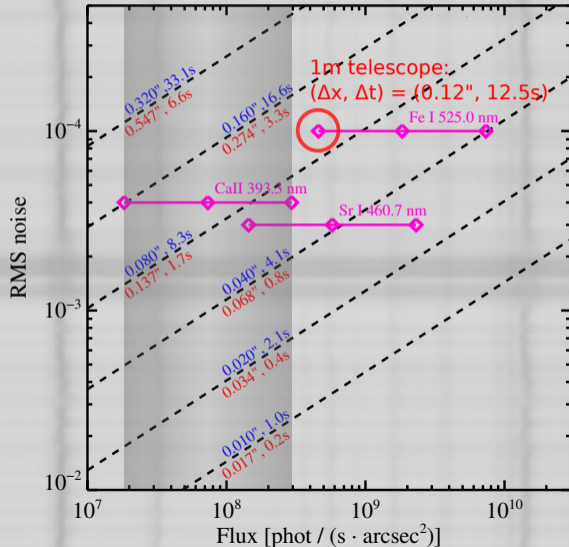
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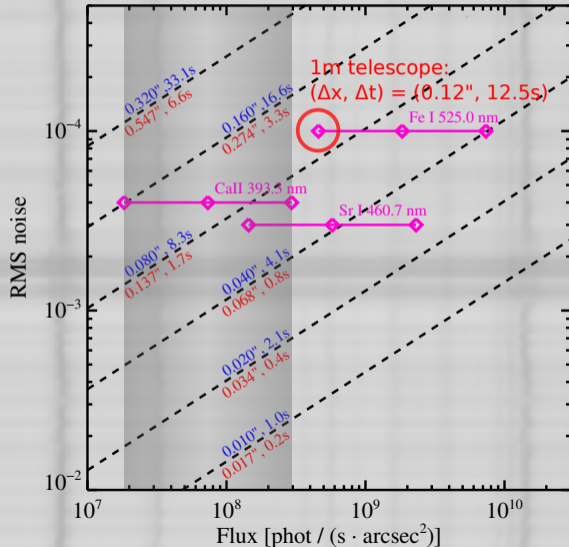
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in near-UV, visible and near-infrared?

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### Extrapolations

- based on photospheric magnetograms
- including chromospheric proxies

→ Thomas Wiegmann  
(Tuesday afternoon)

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### Lyman- $\alpha$

#### Chromospheric Lyman-Alpha SpectroPolarimeter (CLASP)

- 1211–1221 Å
- Stokes *IQU*
- 550''  $\times$  550''
- 2''/2 resolution
- launch: Aug 2015

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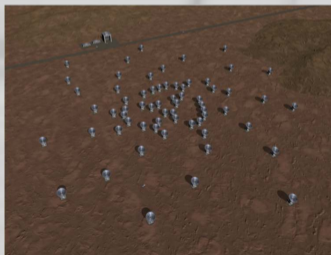
### mm and sub-mm regime

Radio measurements with the Atacama Large Millimeter/Submillimeter Array ALMA

# ALMA - Atacama Large Millimeter/Submillimeter Array

## ALMA basics

- $\approx 50$  operational antennas, moveable to  $\approx 185$  different pads
- spatial res.:  $\leq 0''.01$  @  $850 \mu\text{m}$

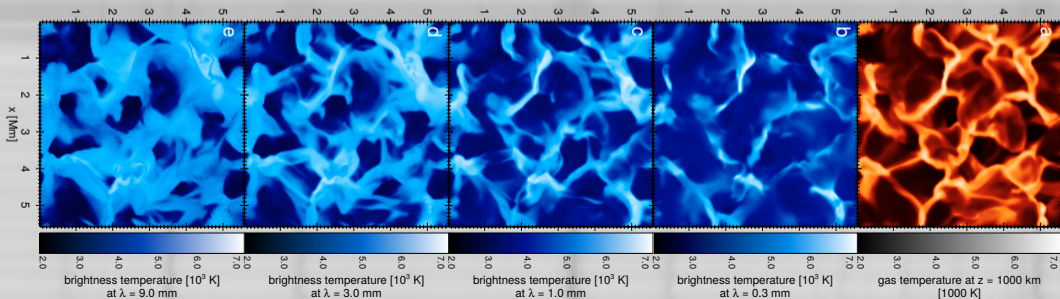




# ALMA - Atacama Large Millimeter/Submillimeter Array

## ALMA measurement

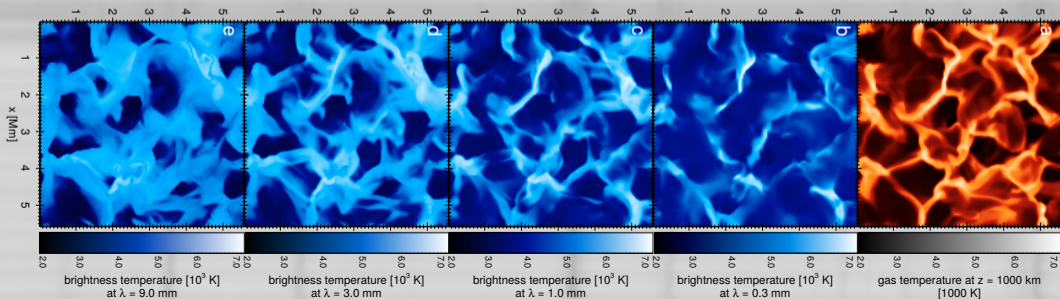
- bremsstrahlung from  $e^-$  interacting with ions / H (thermal free-free /  $H^-$  opacity)
  - $e^-$  in LTE  $\rightarrow$  Planck source function
  - Rayleigh-Jeans approx. highly accurate
- $\rightarrow$  "thermometer" to probe the solar atmosphere



# ALMA - Atacama Large Millimeter/Submillimeter Array

## ALMA for chromospheric B?

- B influences T distrib. by suppressing power of prop. waves
- Zeeman polarimetry:
  - high-n recombination lines of H
  - molecules (CH, CN, CO, NaH)



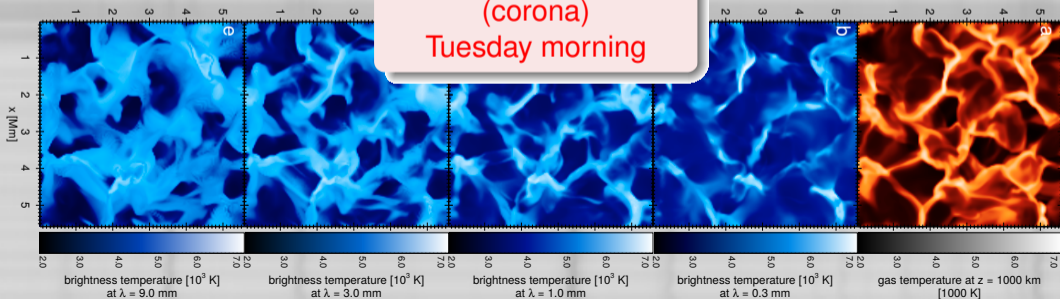
Wedemeyer-Böhm et al. (2007)

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Stephen White  
(corona)  
Tuesday morning



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## Chromospheric Lines

Mg II h

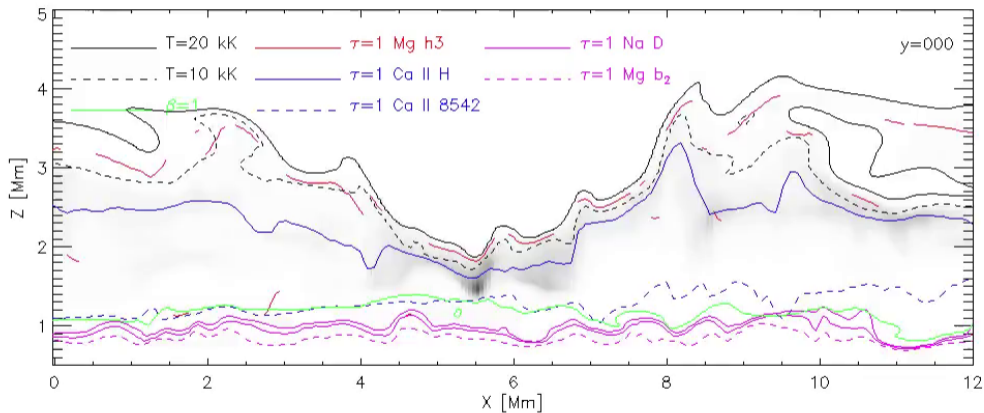
He I 10830

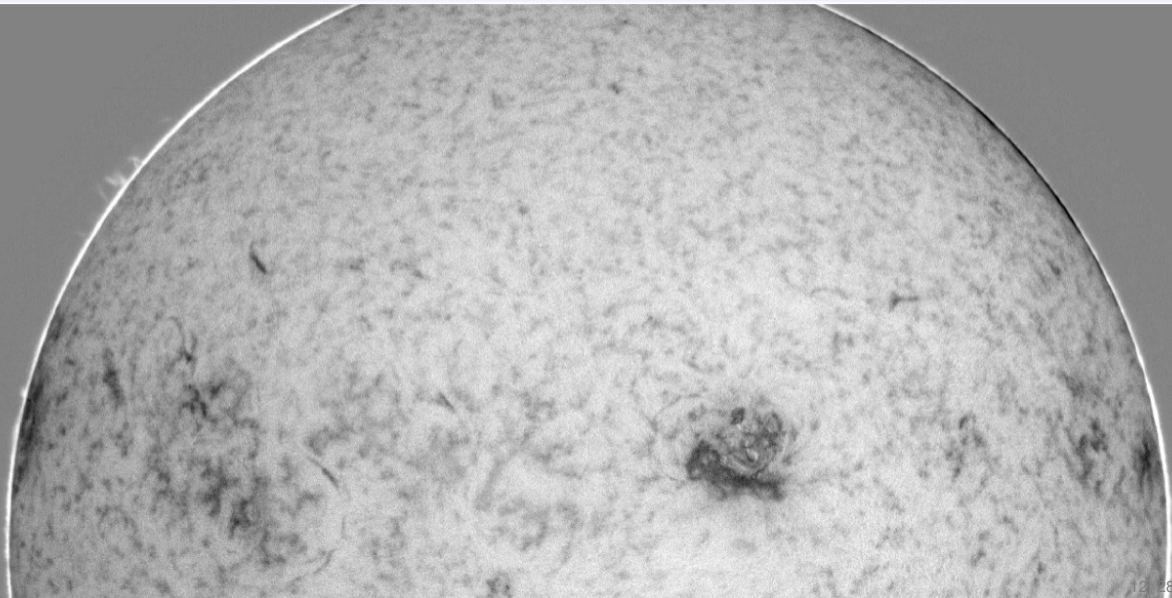
Ca II H

Ca II IR

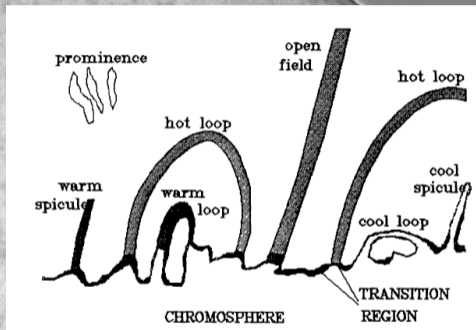
Mg I b

Na D



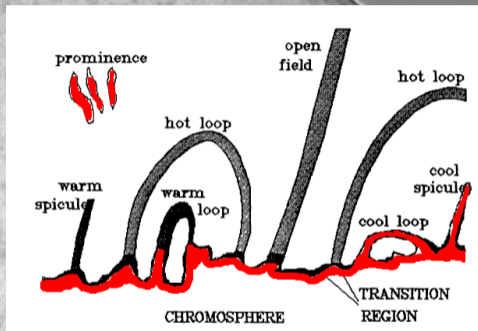


# He I – Formation Height



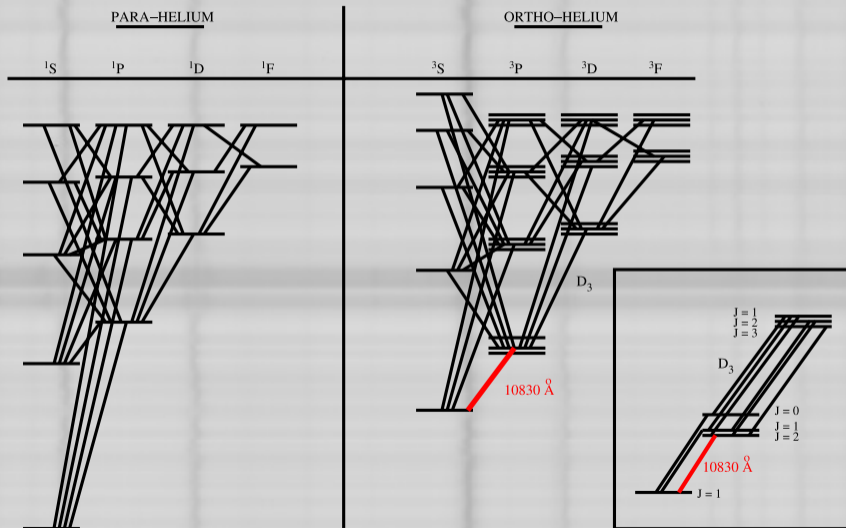
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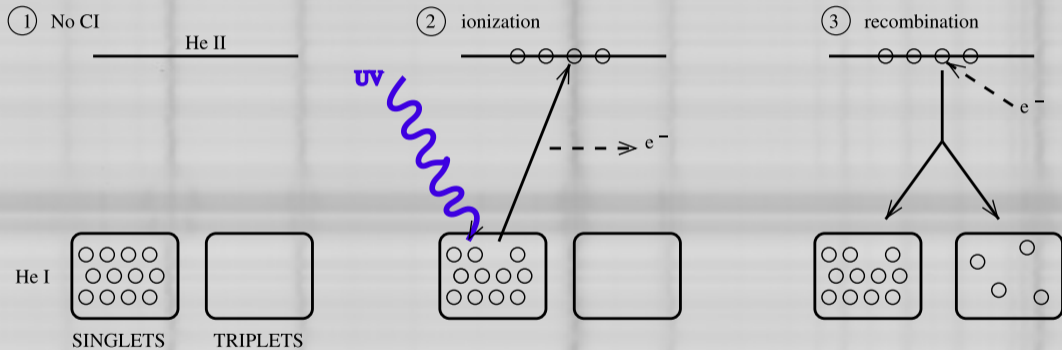
Avrett et al. (1994)

## The He I atom (Centeno et al., 2008)





## Coronal Illumination - Ionization - Recombination (Centeno et al., 2008)



## Recent He I 10830 Å Hi-Res Spectropolarimeters

**SPINOR @ DST (Sac Peak)**

Socas-Navarro et al. (2006)

- full Stokes simultaneous obs. of several VIS + IR regions
- virtually any combination of spectral lines possible

**FIRS @ DST (Sac Peak)**

Jaeggli et al. (2010); Schad (2013)

- 4-slit, dual-beam spectropol.
- Fe I 6302 & He I 10830
- simultaneous with IBIS

**NIRIS @ 1.6m NST (Big Bear)**

Cao et al. (2012)

- attached to 1.6 m NST at Big Bear
- dual Fabry-Pérot Interferometers
- imaging polarimetry @ 0.''25

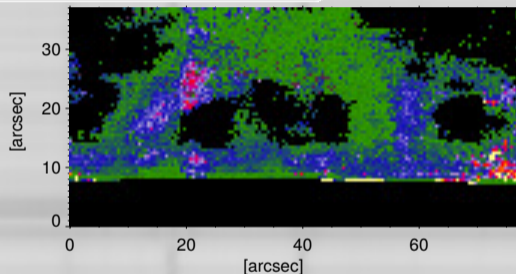
**GRIS @ 1.5m GREGOR (Tenerife)**

Collados et al. (2012)

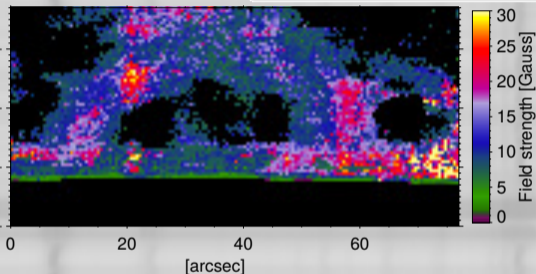
- attached to 1.5 m GREGOR telescope (Tenerife)
- standard Czerny-Turner config.
- spectro-polarimetry @ 0.''25

The magnetic field configuration of a solar prominence inferred from spectropolarimetric observations in the He I 10830 Å triplet (Orozco Suárez et al., 2014)

quasi-horizontal solution



quasi-vertical solution



## HAZEL inversions (Asensio Ramos et al., 2008)

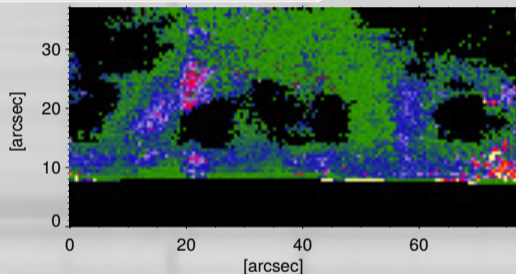
70 s/slit pos

Ambiguities (unresolved, plausibility argument: use quasi-horizontal solution):

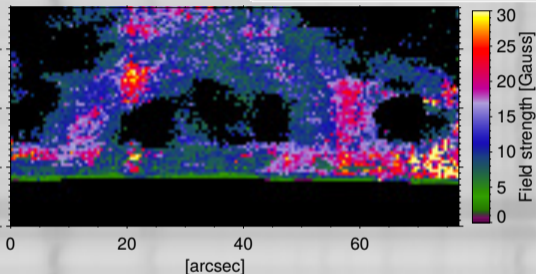
- Zeeman effect:  $180^\circ$  ambiguity
- Hanle effect:  $90^\circ$  and  $180^\circ$  ambiguity

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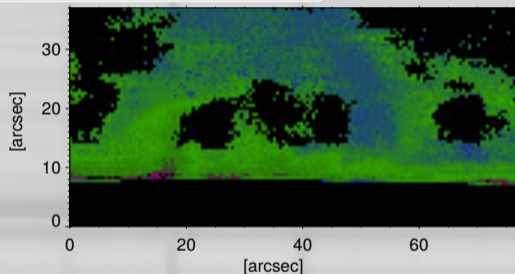


### Magnetic field strength

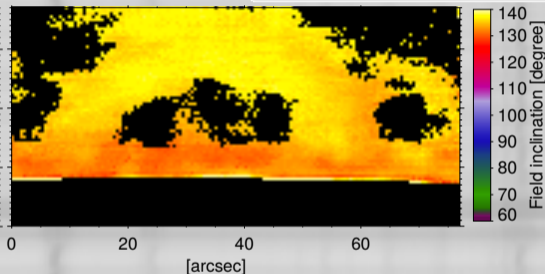
- quiescent prominence, on average 7 G
- up to 30 G at prominence feet (coinciding with high opacity)

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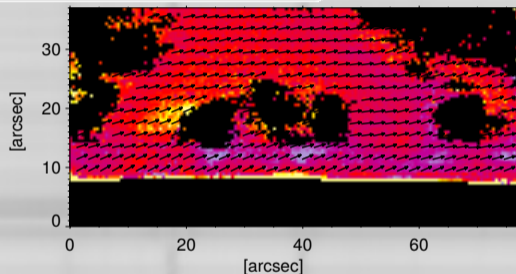


## Magnetic field inclination

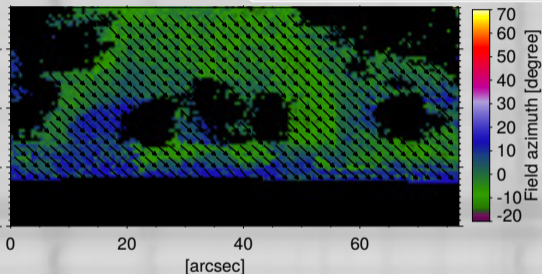
- inclined  $\approx 77^\circ$  to solar vertical;  
in between previous results:  $60^\circ$  (e.g., Bommier et al., 1994) and horizontal (Casini et al., 2003)

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quasi-horizontal solution



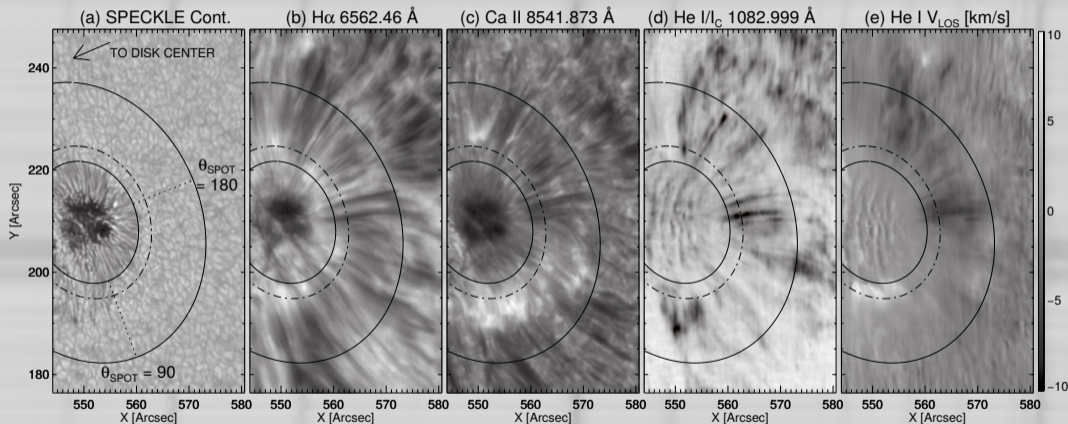
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### Magnetic field orientation wrt. prominence axis

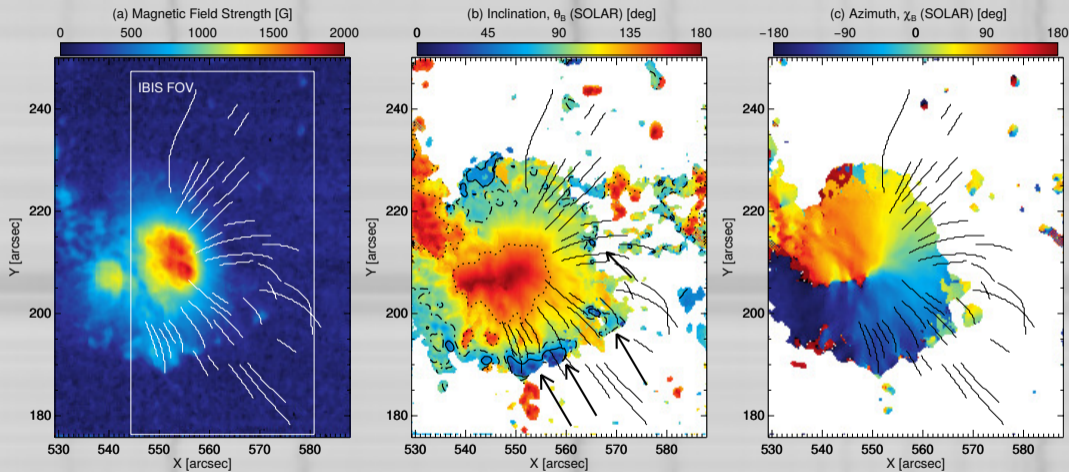
- inclined  $\approx 58^\circ$  /  $\approx 156^\circ$  to prominence long axis (unresolved ambiguity), both solutions: inverse polarity prominence

## He I Vector Magnetometry of Field-aligned Superpenumbral Fibrils (Schad et al., 2013)



IBIS & FIRS Observations, NOAA AR 11408, Jan 29 2012,  $\mu = 0.8$

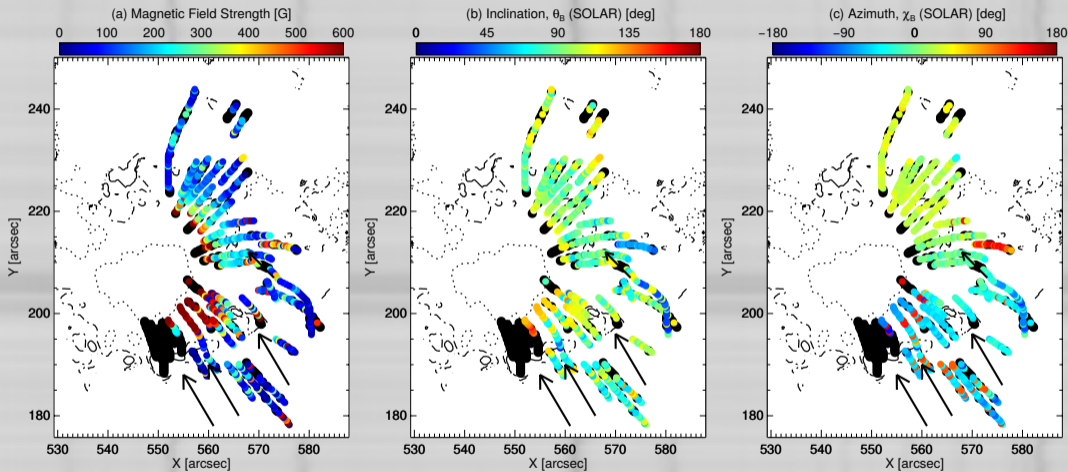
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Photospheric field from Si I ME-inversions (HELIX<sup>+</sup> Lagg et al., 2009)

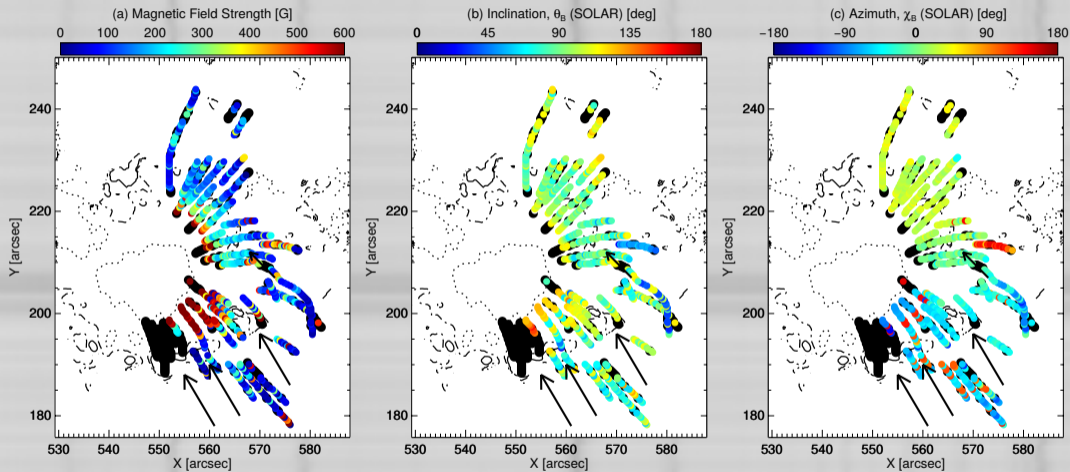


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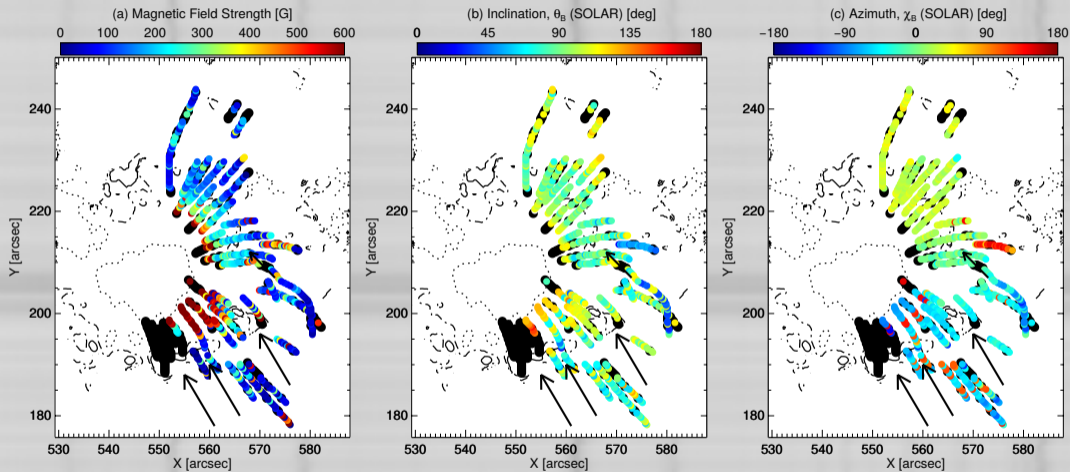
Fibril tracing (CRISPEX, Vissers & Rouppe van der Voort, 2012), careful disambiguation (Hanle & Zeeman), assumption on fibril height (1.75 Mm)

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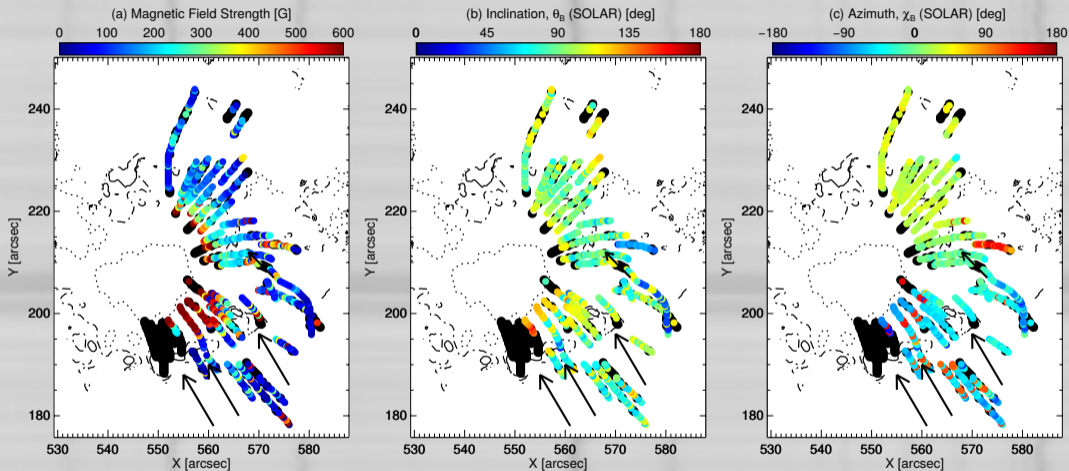
B-strength: rise in strength towards inner endpoints

## He I Vector Magnetometry of Field-aligned Superpenumbral Fibrils (Schad et al., 2013)



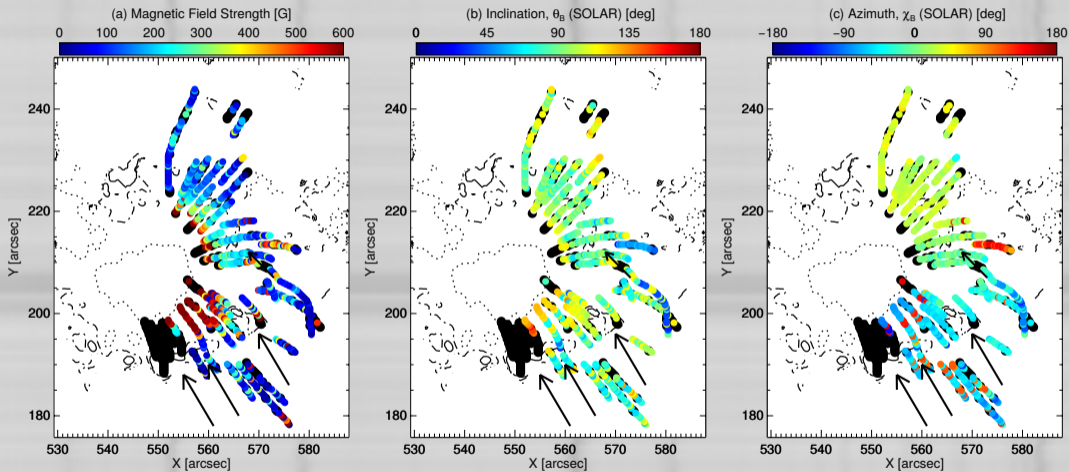
B-inclination: change at inner endpoint towards sunspot

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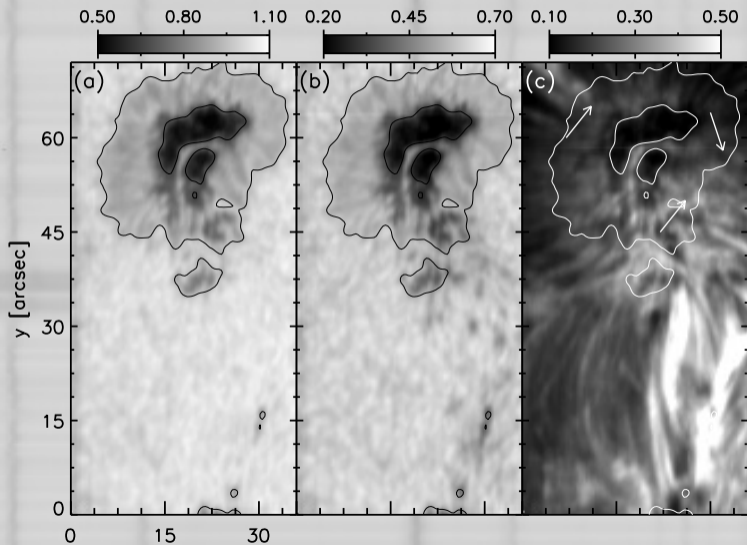
B-inclination: remain horizontal until outer endpoint  
 few fibrils: turn over again, connect in regions of opposite polarity photosphere

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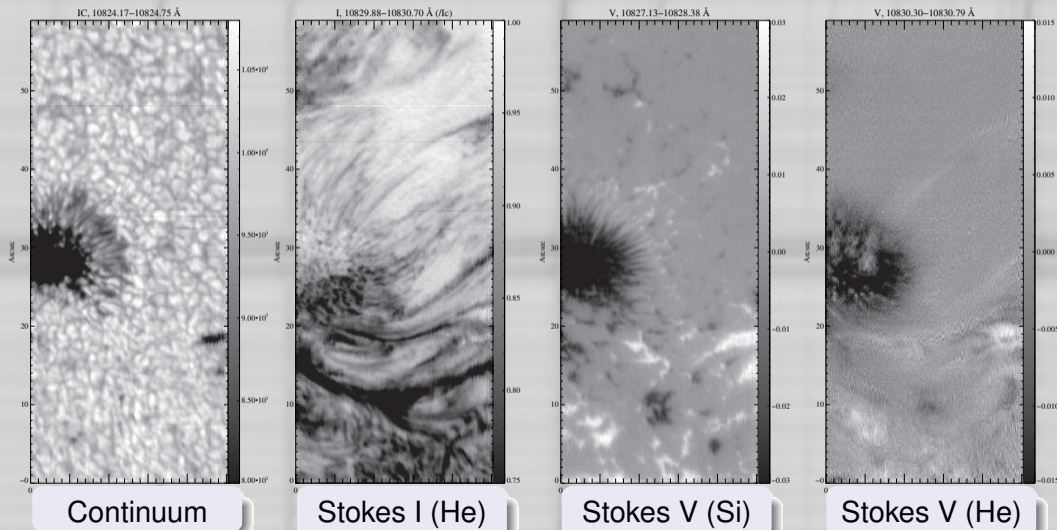


B-azimuth: aligned  $\pm 10^\circ$  with fibrils  
 fibrils carry inverse Evershed flow

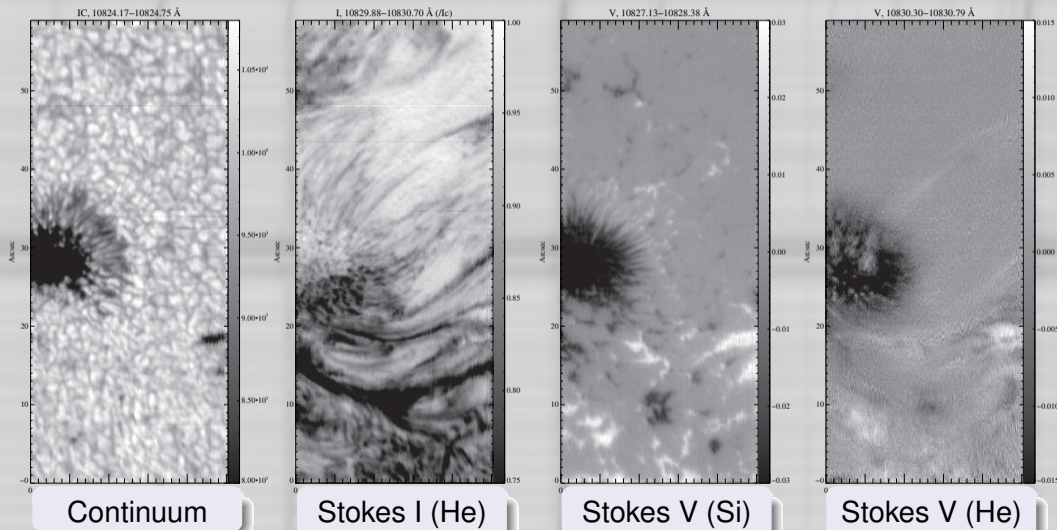
## Comparison: High-res until 2013 (PhD thesis: Joshi, 2014)



# GREGOR/GRIS Data & First Results (June 2014)

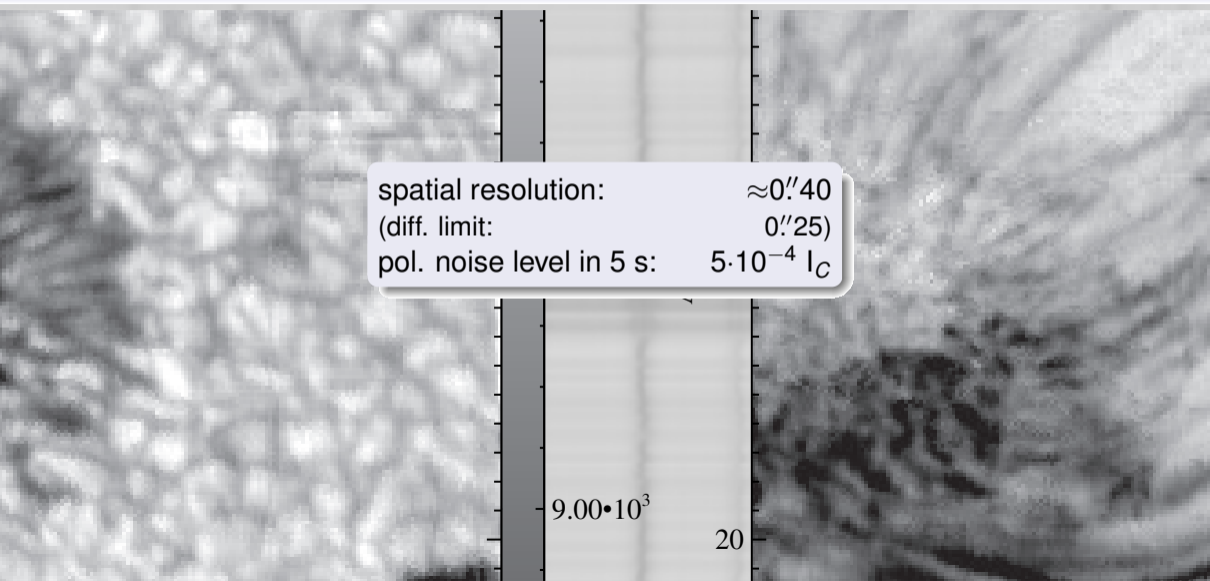


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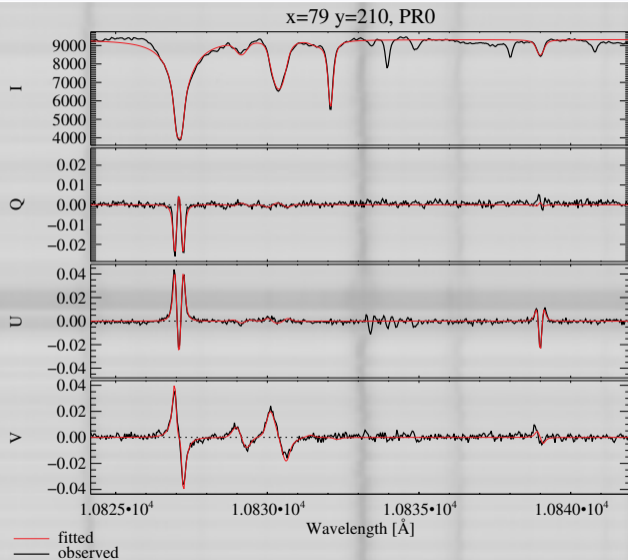




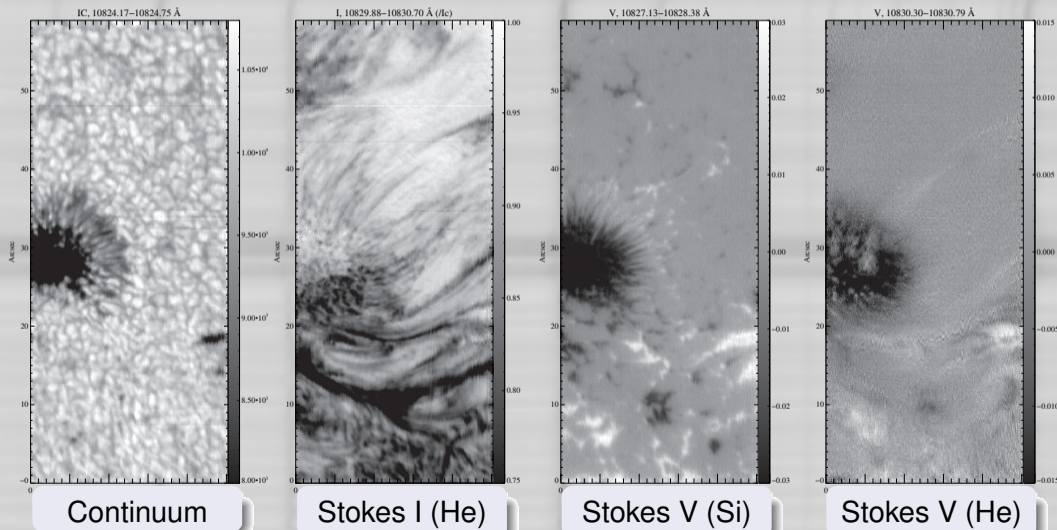
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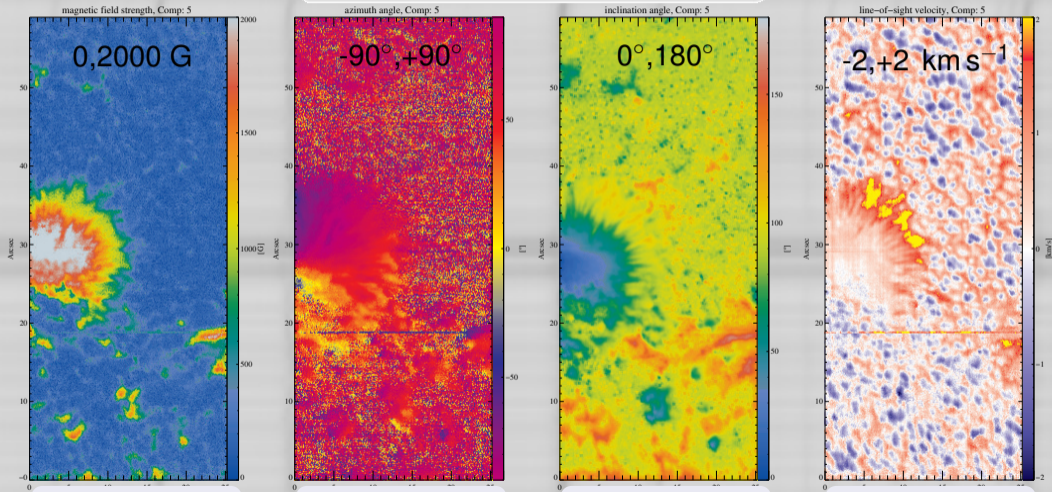


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## Ca I – deep photosphere



B-strength

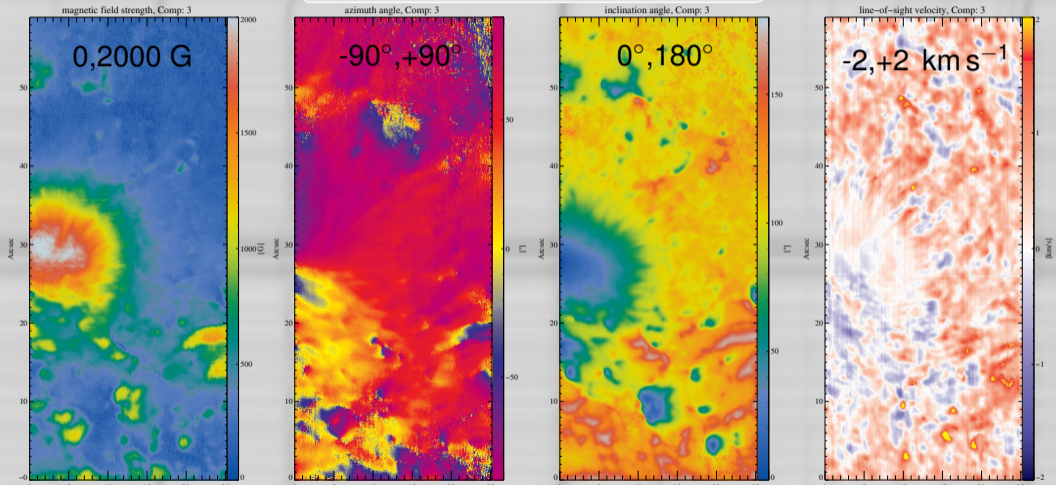
Azimuth

Inclination

LOS-velocity

# GREGOR/GRIS Data & First Results (June 2014)

## Si I – mid/upper photosphere



B-strength

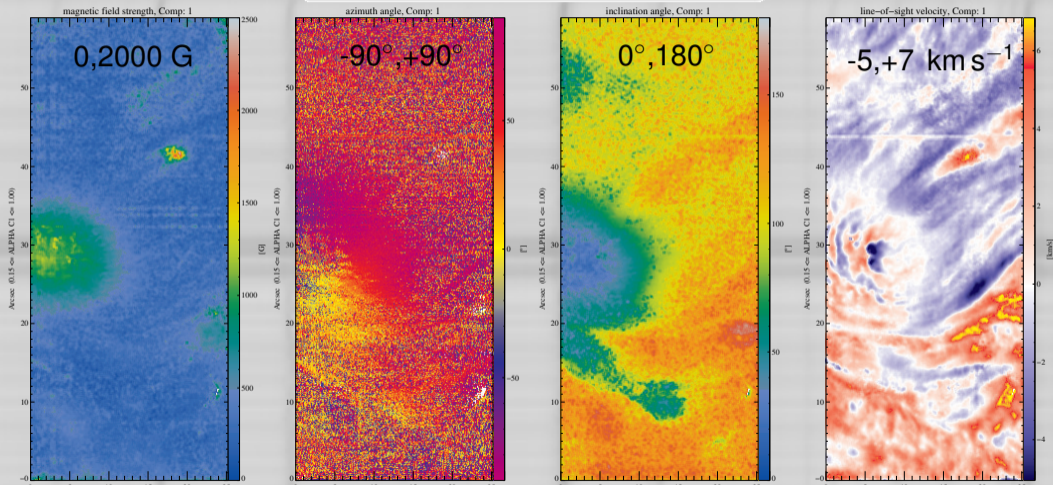
Azimuth

Inclination

LOS-velocity

# GREGOR/GRIS Data & First Results (June 2014)

## He I – upper chromosphere



B-strength

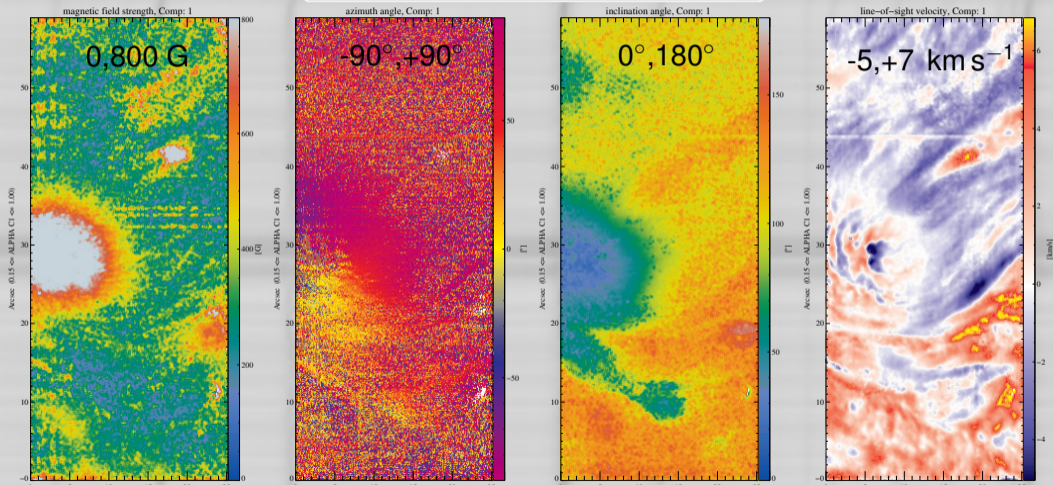
Azimuth

Inclination

LOS-velocity

# GREGOR/GRIS Data & First Results (June 2014)

## He I – upper chromosphere



**B-strength**

**Azimuth**

**Inclination**

**LOS-velocity**

## Chromospheric Fine Structure: Summary

## Fine structure in the He I spectral region

- fine structure mainly He I intensity - almost absent in Stokes *QUV* images / B-vector
- continuous decrease of fine structure in B with height:
  - Ca I (deep photosphere): 0''40
  - Si I (mid/upper photosphere): 0''70
  - He I (chromosphere): 1''00

→ Does the magnetic field loose the fine structure?

→ Does the Stokes / fine structure only outline velocity and density/temp. fluctuations?

→ Is the sensitivity of the measurement too low to detect the fine structure?



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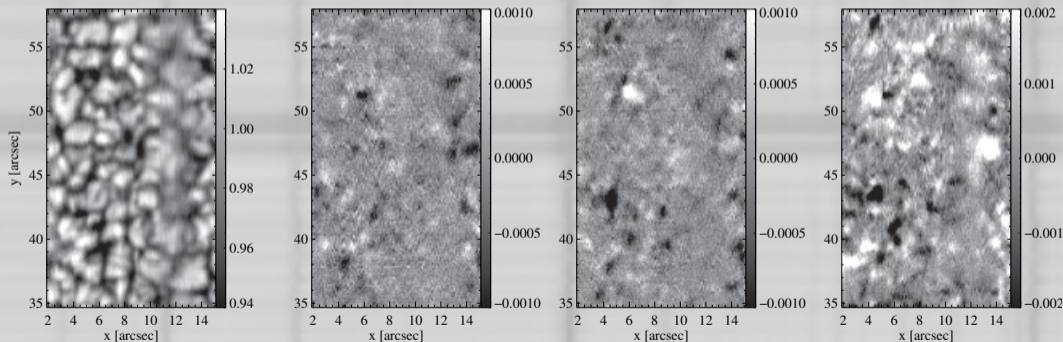
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- Does the magnetic field loose the fine structure?
- Does the Stokes *I* fine structure only outline velocity and density/temp. fluctuations?
- **Is the sensitivity of the measurement too low to detect the fine structure?**

## GREGOR/GRIS: Higher quality He I observation soon...

GREGOR/GRIS data at Fe I  $1.56 \mu\text{m}$  (sep 2014):  
 $0.35''$  ( $\approx$  diff. limit) @  $3\text{--}5 \cdot 10^{-4} I_C$

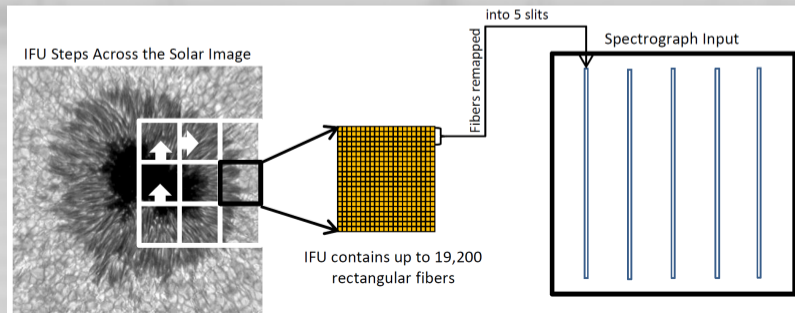


# Ground-based: DKIST

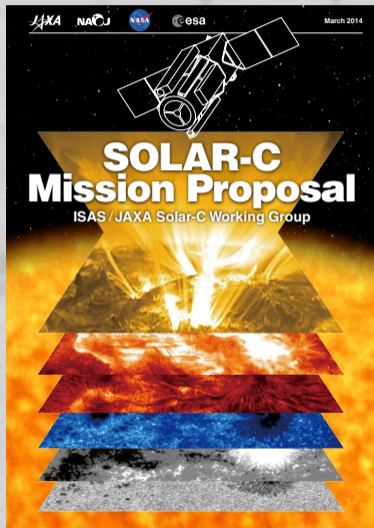
## DL-NIRSP @ DKIST


The Diffraction Limited Near-Infrared Spectropolarimeter; Haosheng Lin


Spectral Range:	5000 Å – 18000 Å
Spectral resolution:	up to 250000
Spatial resolution:	0.07" @10830Å
Target polarimetric accuracy:	$> 5 \cdot 10^{-4} I_c$



# Future He I 10830 Å observatory

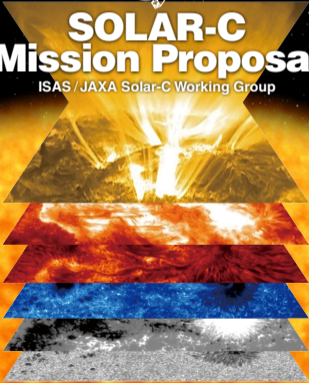



March 2014



## SOLAR-C Mission Proposal

ISAS / JAXA Solar-C Working Group



## Solar-C / EPIC

1.4 m solar telescope in GSO

- spectropolarimetry in He I 10830, Ca II IR, Mg II h&k, Fe I 525
- *IQUV* @ 0.07''–0.14''
- target:  $10^{-4}$
- EPIC (ESA): Jan 15 2015
- Solar-C (JAXA): Feb 2015
- launch 2022–2025





## EPIC

### European Participation In Solar-C

A proposal in response to the M4 mission opportunity of ESA  
 S.K. Solanki and the EPIC consortium



## Scientific future of He I 10830

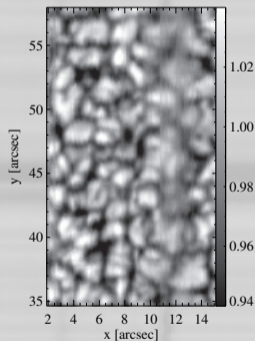
**To-Do list for He I 10830 Science**

- obtain measurements at highest possible spatial resolution, S/N in the low  $10^{-4}$  range (ideal: 2D FOV)
- reliable disambiguation methods (Van Vleck ambiguity,  $180^\circ$  Hanle & Zeeman ambiguity):  
→ combination with other chromospheric line?
- reliable anisotropy determination (take into account coronal illumination, symmetry breaking due to, e.g., sunspots):  
→ determine population imbalances
- reliable height determination: → high S/N, stereoscopy

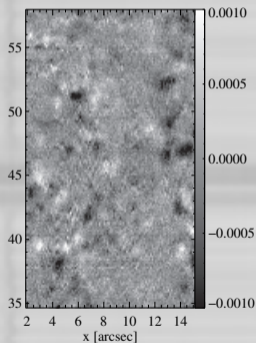
# Very quiet sun region (2014-Sep-08)

All pixels

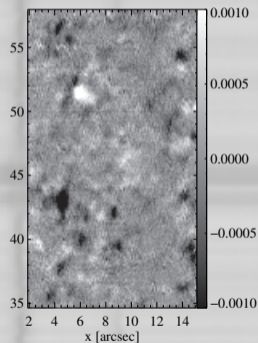
$I_C$



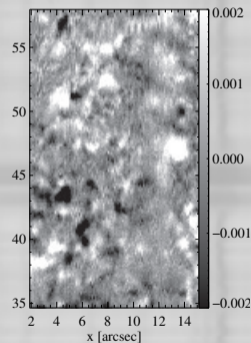
Q



U



V

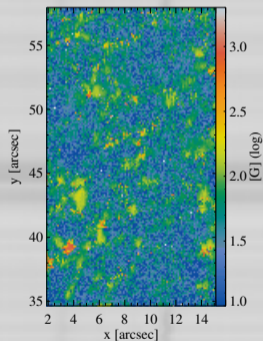




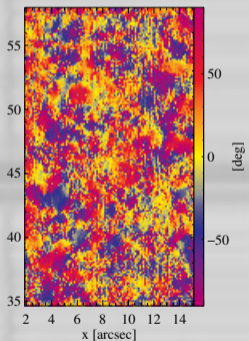
# Very quiet sun region (2014-Sep-08)

All pixels

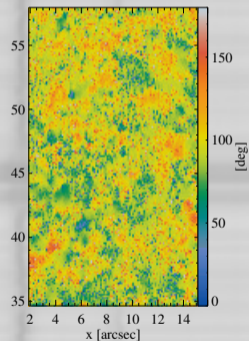
B



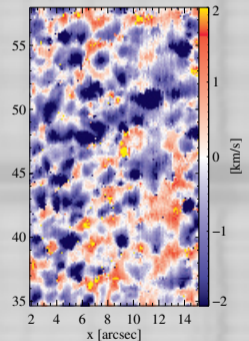
AZI



INC



$v_{LOS}$



# Very quiet sun region (2014-Sep-08)

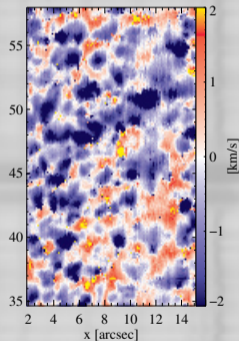
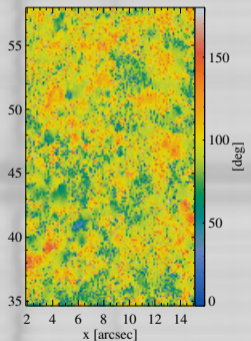
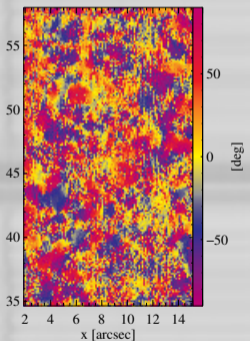
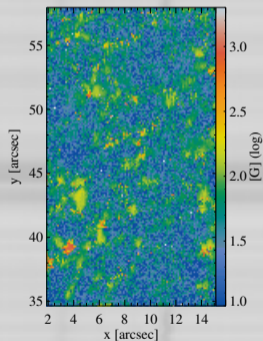
All pixels

B

AZI

INC

$v_{LOS}$



remove all pixels with tot. pol  $\leq 3\sigma$   
 Survival of IG lanes or granules?

# Very quiet sun region (2014-Sep-08)

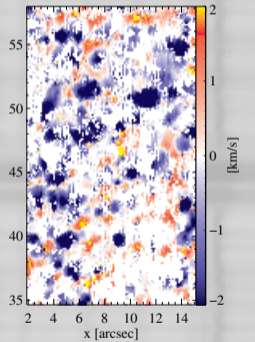
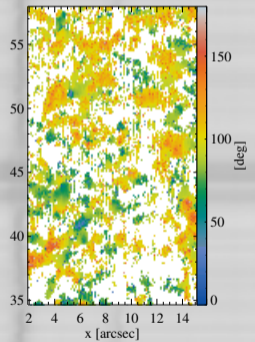
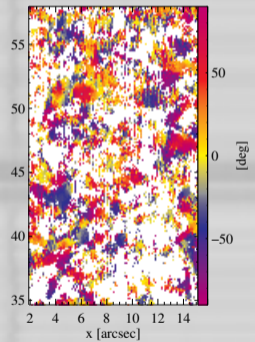
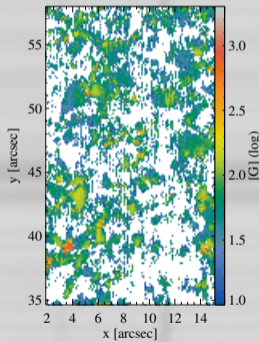
Tot. Pol  $> 3\sigma$

B

AZI

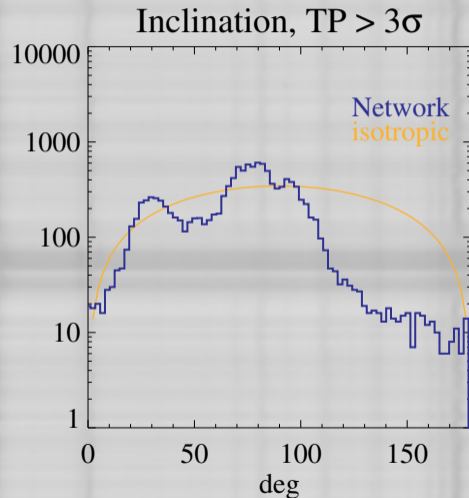
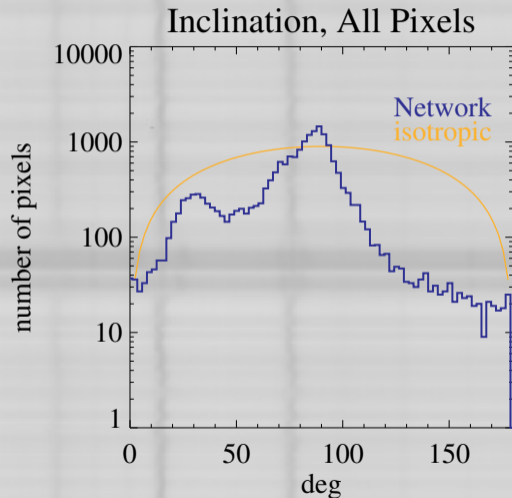
INC

$v_{LOS}$



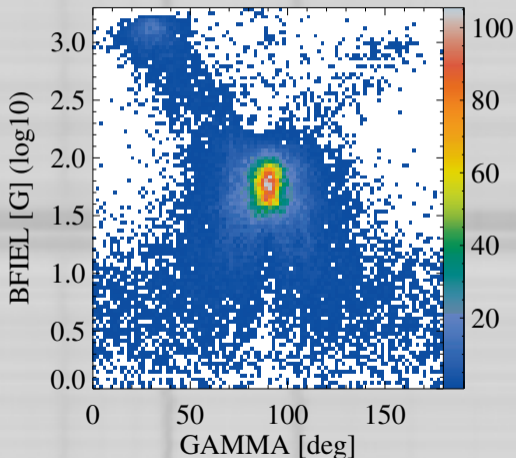
Mainly granules!  
... and some IG lanes

# Distribution: Inclination

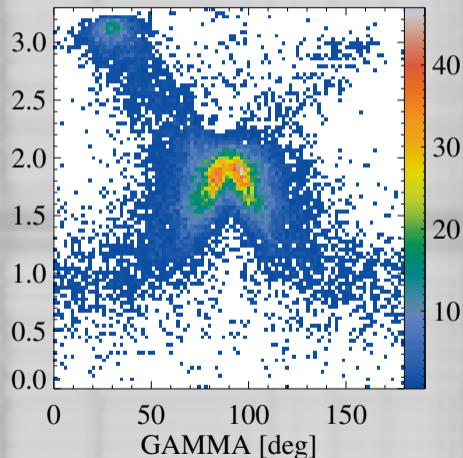


# Distribution: B & Inclination

All Pixels



TP > 3 $\sigma$



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